## 1-5 Solving Inequalities.notebook

1-5: Solving Inequalities
Objective for the day: Students will solve, graph and write inequalities
Key Vocab:
Compound inequality: two inequalities joined together with the word and or the word or

Key Concept Writing and Graphing Inequalities
Inequality Word Sentence
$x>4 \quad x$ is greater than 4.
$x \geq 4 \quad x$ is greater than or equal to 4.
$x<4 \quad x$ is less than 4.
$x \leq 4$
$x$ is less than or equal to 4 .
Graph
$\underset{-1}{1} \begin{array}{llllllll}1 & 1 & 1 & 1 & 9 & & 4\end{array}$
$\begin{array}{llllllll}-1 & 1 & 1 & 1 & 1 & & \\ -1 & 0 & 1 & 2 & 3 & 4 & 5\end{array}$
$\xrightarrow[-1]{+1} \begin{array}{llllllll}-1 \\ -1 & 0 & 1 & 2 & 3 & 4 & 5\end{array}$
$\underset{-1}{ } \mathrm{H}_{-1}$

## Properties Properties of Inequalities

Let $a, b, c$ and $d$ represent real numbers.
Property $\quad$ Definition Example
Transitive If $a>b$ and $b>c$, then $a>c . \quad 5>3$ and $3>1$, so $5>1$
Addition If $a>b$, then $a+c>b+c . \quad 4>2$, so $4+1>2+1$
Subtraction If $a>b$, then $a-c>b-c . \quad 7>4$, so $7-3>4-3$
Multiplication If $a>b$ and $c>0$, then $a c>b c . \quad 6>5$ and $3>0$, so $6(3)>5(3)$ If $a>b$ and $c<0$, then $a c<b c . \quad 3>2$ and $-4<0$, so $3(-4)<2(-4)$
Division If $a>b$ and $c>0$, then $\frac{a}{c}>\frac{b}{c} . \quad 9>3$ and $3>0$, so $\frac{9}{3}>\frac{3}{3}$ If $a>b$ and $c<0$, then $\frac{a}{c}<\frac{b}{c} . \quad 12>6$ and $-6<0$, so $\frac{12}{-6}<\frac{6}{-6}$

I DO

## Example 1

What inequality represents the sentence, "The product of 7 and a number is no more than 50 ?"

$$
7 x \leq 50
$$

WE DO:
What inequality represents the sentence, "The product of 6 and a number is less than 20 "?

$$
6 x<20
$$

I DO:
Example 2
What is the solution of $\widehat{4(x-7)}>-20$ ? Graph the solution.


WE DO:
What is the solution of $-5 \overparen{(2 x-1)+3} 5$
Graph the solution.


$$
-10 x \leq-10
$$

$$
x \geq 1
$$

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I DO:
Example 3
Plumber A charges $\$ 75$ for a service charge and $\$ 40$ per hour.
Plumber B charges $\$ 50$ per hour but no service charge. How
many hours must a plumbing job last for Plumber A to cost less than Plumber B?

$$
\begin{gathered}
75+40 x<50 x \\
75<10 x
\end{gathered}
$$

WE DO: $\quad 7.5<x$
Do you UNDERSTAND? Eastside Gym charges a $\$ 60$ initial fee and $\$ 28.50$ per month. Valley Gym charges $\$ 36$ per month, and no initial fee. After how many months of use would Eastside cost less than Valley?

$$
\begin{gathered}
60+28.5 x<36 x \\
60<7.5 x \\
8<x \\
\hline 0.38: 10-23,27
\end{gathered}
$$

